MAT2500-03/04 10S Quiz 2 Print Name (Last, First) $\qquad$
Show all work, including mental steps, in a clearly organized way that speaks for itself. Use proper mathematical notation, identifying expressions by their proper symbols (introducing them if necessary), and use arrows and equal signs when appropriate. Always simplify expressions. BOX final short answers. LABEL parts of problem. Keep answers EXACT (but give decimal approximations for interpretation). Indicate where technology is used and what type (Maple, GC).

Given three points $\mathrm{P}_{1}(1,1,0), \mathrm{P}_{2}(1,2,1), \mathrm{P}_{3}(2,1,2)$ and the parallelopiped formed from their three position vectors $\overrightarrow{\boldsymbol{r}}_{1}, \overrightarrow{\boldsymbol{r}_{2}}, \overrightarrow{\boldsymbol{r}_{3}}$.
a) Write the parametrized equations of the line $L_{1}$ through the point $P_{1}$ parallel to the position vector $\overrightarrow{\boldsymbol{r}}_{2}$.

b) Find a normal vector $\overrightarrow{\boldsymbol{n}}$ for the for the plane $\mathbb{P}_{1}$ which contains the right outside face of the parallelepiped shown in the figure.
c) Write the simplified equation for this plane.
d) Let $\overrightarrow{\boldsymbol{b}}=\overrightarrow{\boldsymbol{r}}_{1}+\overrightarrow{\boldsymbol{r}}_{2}+\overrightarrow{\boldsymbol{r}}_{3}$ be the main diagonal of the parallepiped. Find the length $b_{p a r}$ of its projection along the vector $\overrightarrow{\boldsymbol{r}}_{3}$.
e) Evaluate $\left|\overrightarrow{\boldsymbol{r}_{3}} \times \overrightarrow{\boldsymbol{b}}\right|$ and then $b_{\text {perp }}=\left|\overrightarrow{\boldsymbol{r}_{3}} \times \overrightarrow{\boldsymbol{b}}\right| /\left|\overrightarrow{\boldsymbol{r}_{3}}\right|$.
[This is the scalar projection perpendicular to $\overrightarrow{\boldsymbol{r}}_{3}$.]
f) Does $b_{\text {par }}^{2}+b_{\text {perp }}^{2}=|\overrightarrow{\boldsymbol{b}}|^{2}$ as it should?

## solution

