MAT2705-01/02 13F Quiz 8 Print Name (Last, First)	
Show all work, including mental steps, in a clearly organized way that speaks for itself. Use prope	r mathematical
notation, identifying expressions by their proper symbols (introducing them if necessary), and use	arrows and equal
signs when appropriate. Always simplify expressions. BOX final short answers. LABEL parts of p	roblem. Keep
answers EXACT (but give decimal approximations for interpretation). Indicate where technology	gy is used and what
type (Maple, GC).	

- 1. my'' + cy' + ky = 0, y(0) = -5, y'(0) = 20; m = 1/2, c = 2, k = 52. [prime is d/dt]
- a) State Maple's solution of the initial value problem.
- b) Put the DE into standard linear form first. Then identify the values of the damping constant and characteristic time $k_0 = 1/\tau_0$, the natural frequency ω_0 , and the quality factor $Q = \omega_0 \tau_0$, exactly and numerically. Is this underdamped, critically damped or overdamped?
- c) Find the general solution by hand, showing all steps.
- d) Find the solution satisfying the initial conditions, showing all steps.
- e) Give exact and numerical values of the amplitude and phase shift and re-express the sinusoidal factor of this solution in phase-shifted cosine form. [Make sure you use a diagram to justify your values.] State what numerical fraction of a cycle (2π) the phase shift is (i.e., evaluate $\delta/2\pi$) as well as its numerical value in degrees, and whether the cosine curve is shifted left (earlier in time) or right (later in time) on the time line. Explain.
- f) State the two envelope functions of this decaying oscillating solution.
- g) Make a rough sketch of the plot of your solution and its two envelope functions in a viewing window of width 5 times the characteristic time of the solution exponential factor.
- h) What are the numerical values of the periods associated with the natural frequency and the actual frequency of the sinusoidal factor of the solution and how do they compare?

solution