- 1. The curve  $y = -h \ln \left(1 \frac{x}{R}\right)$  over the interval  $0 \le x < R$  is rotated around the x-axis, with h > 0, R > 0.
- a) Let H > 0 designate the average value of y over this interval. Write down a simplified definite integral for H and then evaluate it by hand showing all your steps, and make sure it agrees with Maple's evaluation.
- b) Make a diagram of this curve over this interval and include a horizontal line for this average value. Does the rectangle it makes appear to have the same area as that above the curve? Explain.
- c) Let *V* denote the volume of a solid formed by revolving this curve segment around the *x*-axis, and indicate a typical vertical cross-section of the integration region needed to evaluate this volume, labeling its endpoints appropriately to justify your limits of integration and indicating how you obtained your integrand. Write down a simplified definite integral for *V* and then use Maple to evaluate it.
- d) Compare this solid with a cylinder of revolution about the *x*-axis. What radius would the cylinder need to have for it to have the same volume?

## **solution**