1.a) Use the geometric series algebra manipulation trick and the identity $\ln\left(\frac{2+x}{2-x}\right) + C = \int \frac{4}{4-x^2} dx$ to find

a power series for $f(x) = \ln\left(\frac{2+x}{2-x}\right)$. [Hint: Set C = 0 for the natural power law antiderivatives on the right hand side series.]

- b) What is its radius of convergence?
- c) Use the Taylor series formula $f(x) = \sum_{n=0}^{\infty} \frac{f^{(n)}(0)}{n!} x^n$ to evaluate the cubic Taylor approximation for this

function and compare with the expression from part a) for its first 2 nonzero terms. [Hint: Use Maple to evaluate the necessary derivatives at x = 0.]

d) Does this series converge at the endpoints of the interval of convergence? Explain.

Optional.

e) What does Maple give for the value of your part a) series formula if you first > assume(a < x < b)

where a < x < b is the open interval of convergence?

▶ solution