| MAT2500-01/04 18S Quiz 7 Print Name (Last, First)  |        |
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| Show all work, including mental steps, in a clearly organized way that speaks for itself. Use proper       |        |
| mathematical notation, identifying expressions by their proper symbols (introducing them if necessary), an | ıd use |
| EQUAL SIGNS and arrows when appropriate. Always SIMPLIFY expressions. BOX final short answers.             |        |
| LABEL parts of problem. Keep answers EXACT (but give decimal approximations for interpretation when        | a      |
| appropriate). Indicate where technology is used and what type (Maple, GC).                                 |        |

If the length of the diagonal of a rectangular box must be L, what is the largest possible volume?

Although the result may be obvious from symmetry considerations, respond to this max-min problem as follows. Draw a box indicating the three dimensions x, y, z and indicate their allowed values. Identify the volume function V and use the given constraint to eliminate z and express V as a function f(x, y) and draw a graph of the bounded region of the plane over which this function is positive. Find the single critical point  $(x_0, y_0)$  in the interior of this region and locate it in your diagram [hint: subtract your two first derivative equations to get started in solving them] and then evaluate the volume  $f(x_0, y_0)$  there. This must be the maximum value. Answer the word problem with a complete English sentence describing completely your result. **Optional.** 

Use Maple to evaluate second derivatives at this critical point to confirm that this is a local maximum of the function. This can even be done by hand.

## **▶** solution